

---

# Impedance Localization: HT Studies

R. Calaga, D. Quatraro, G. Rumolo  
Ack: R. Tomás

Imp. Meeting, May 30, 2008

---

# Intensity Dependent Optics

---

Based on EPAC04 Paper: G. Arduini, F. Zimmermann, C. Carli

$$K_{eff} = \frac{eN_b}{2\sqrt{\pi}\sigma_z(E_b/e)} Im\{Z_{\perp,eff}\}$$

To 1<sup>st</sup> order,  $\Delta K$  perturbation with intensity causes:

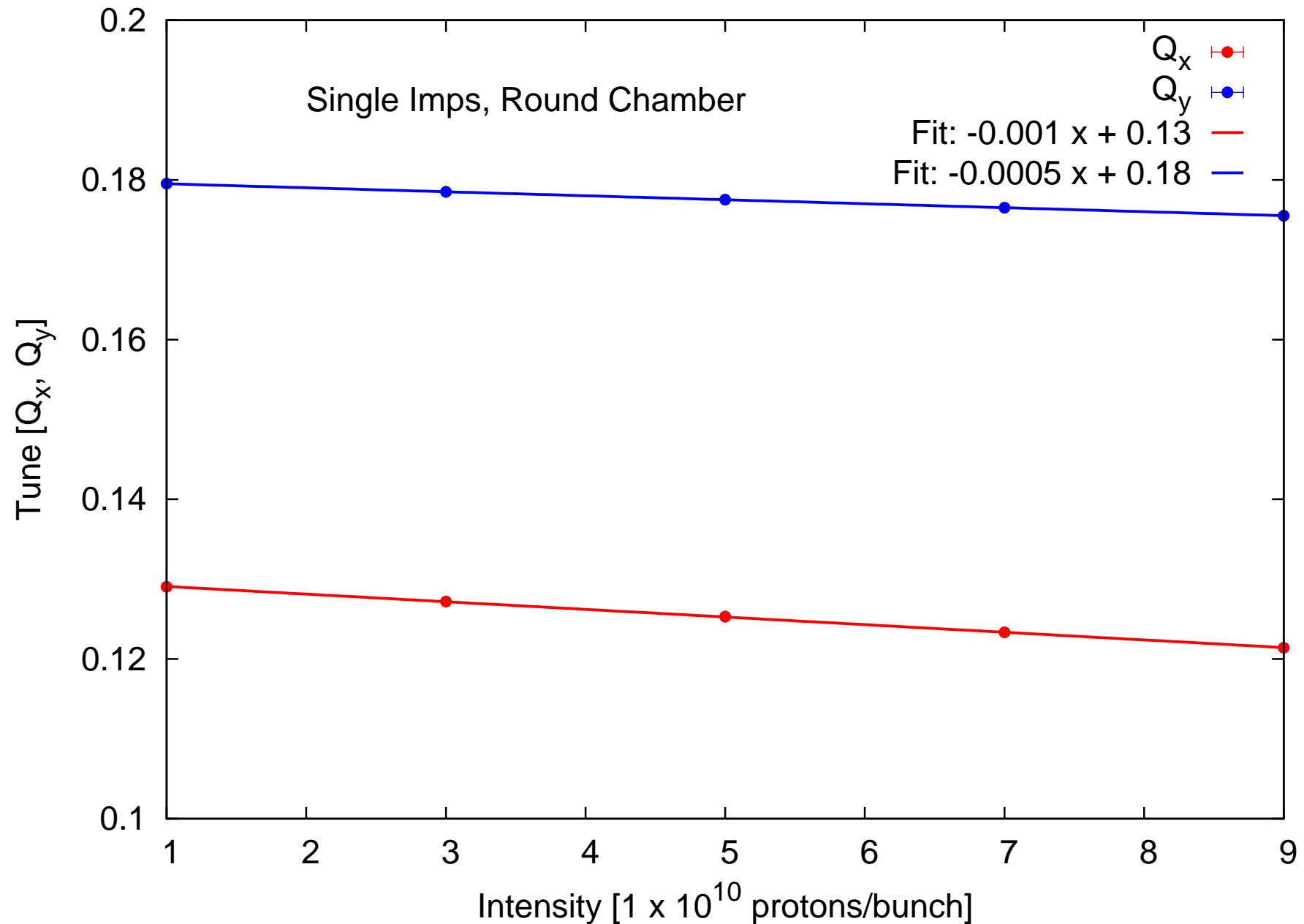
$$\Delta Q = \frac{1}{4\pi} \beta_k \Delta K$$

$$\frac{\Delta \beta(s)}{\beta(s)} = \frac{\beta_k \cos(2|\phi(s) - \phi_k| - 2\pi Q)}{2 \sin(2\pi Q)} \Delta K$$

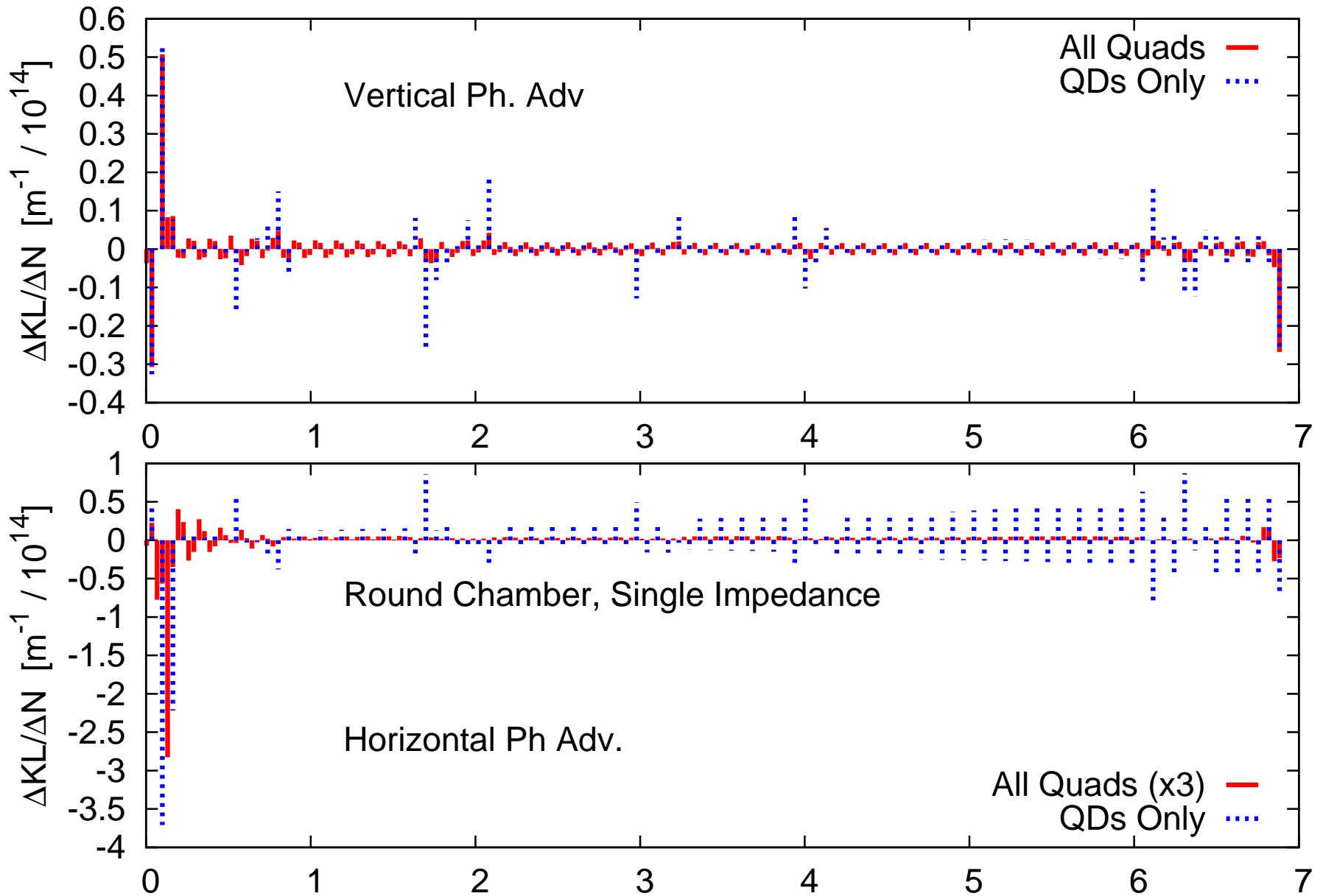
Procedure:

- Measure/Simulate phase advance between BPM pairs for varying intensities
- Linear fit:  $\phi_I = \phi_0 + (\Delta\phi/\Delta N_b)N_b$
- $\Delta K = R^{-1}\{\Delta\phi/\Delta N_b, Q_x, Q_y\}$ , where R is model response matrix

## Case I: Intensity dependent $\Delta Q$ , Single Imp

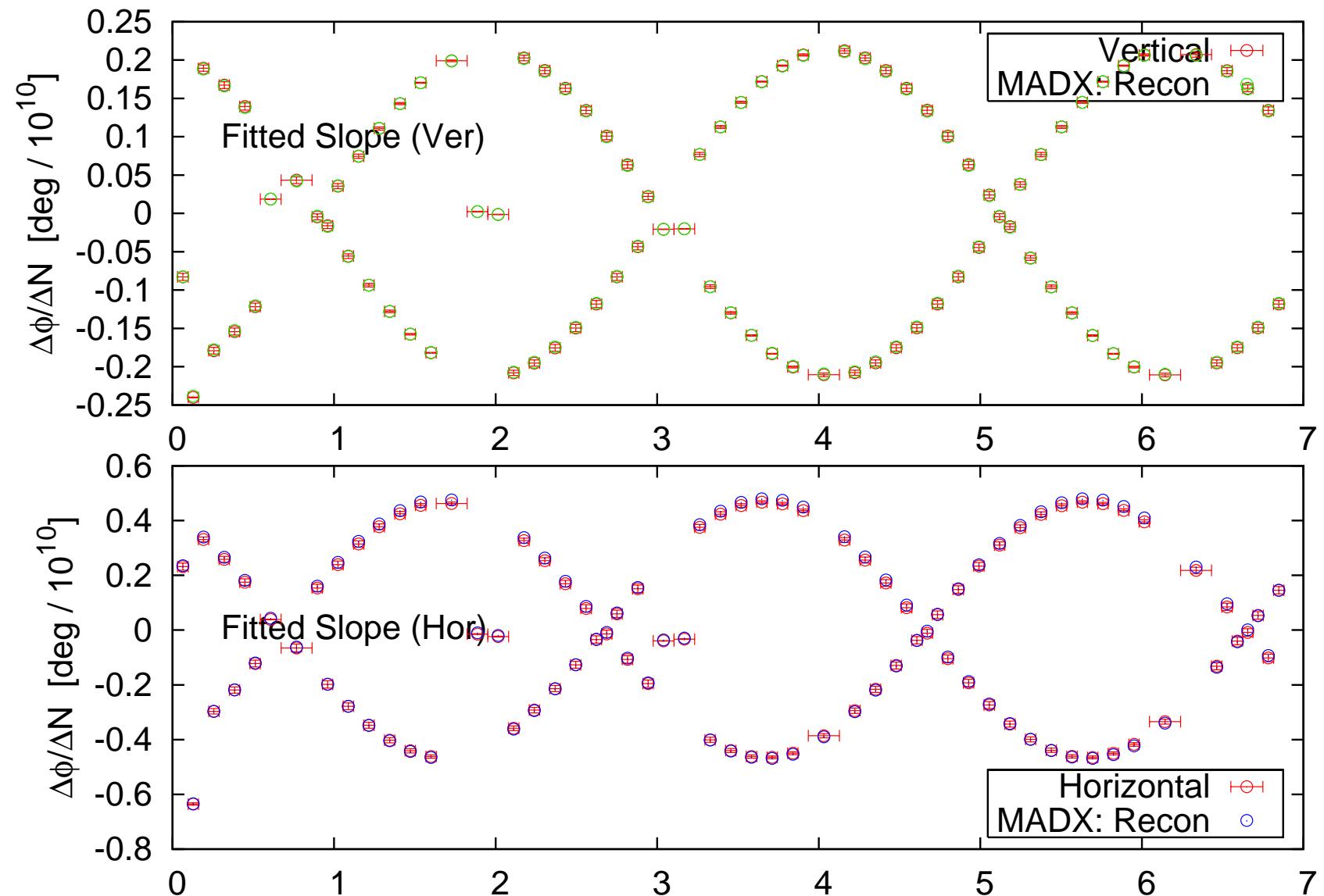


## Recon $\Delta K_i$ , Single Imp

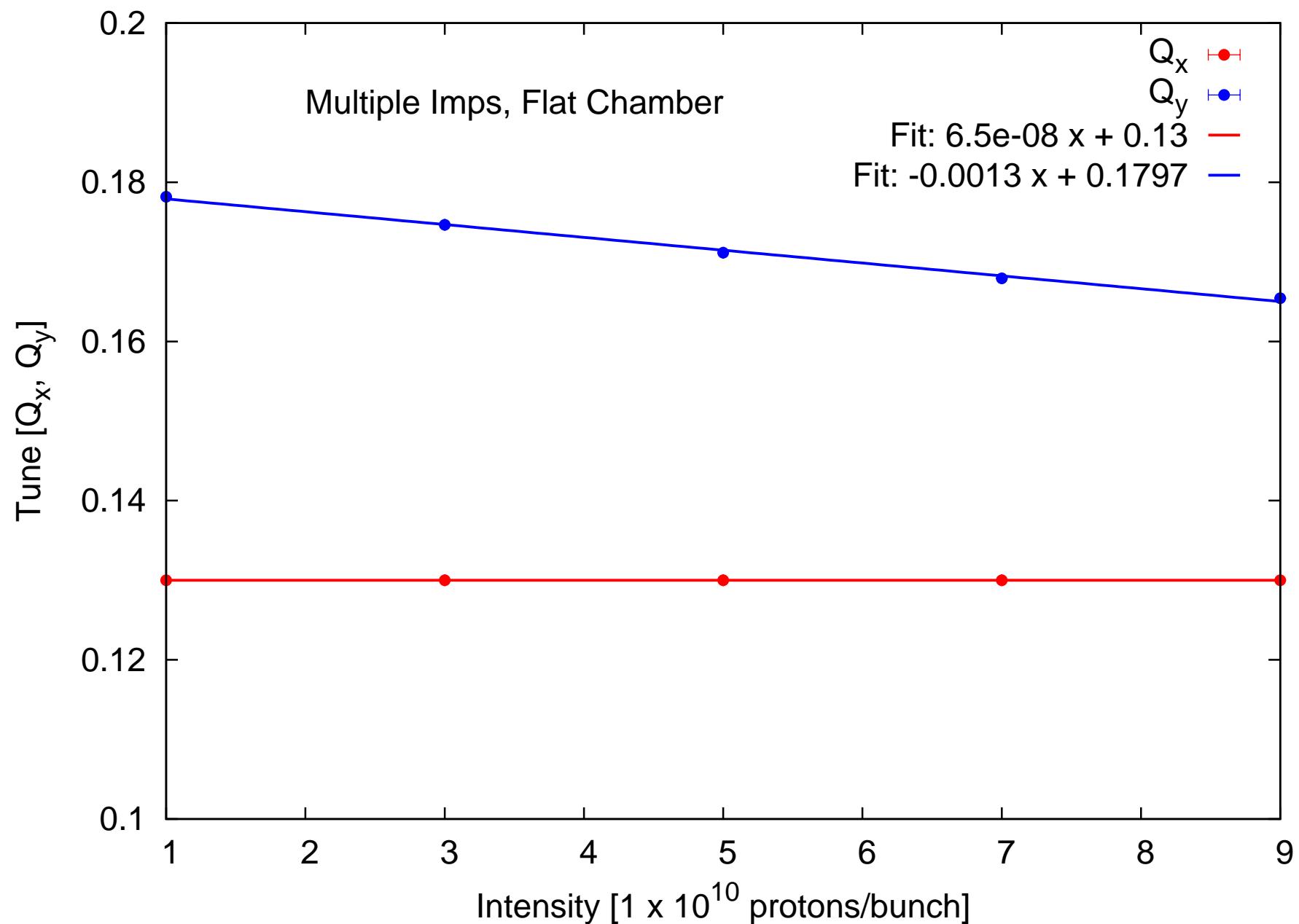


## Intensity Fitted Slope $\{\Delta\phi_{a \rightarrow b}\}$

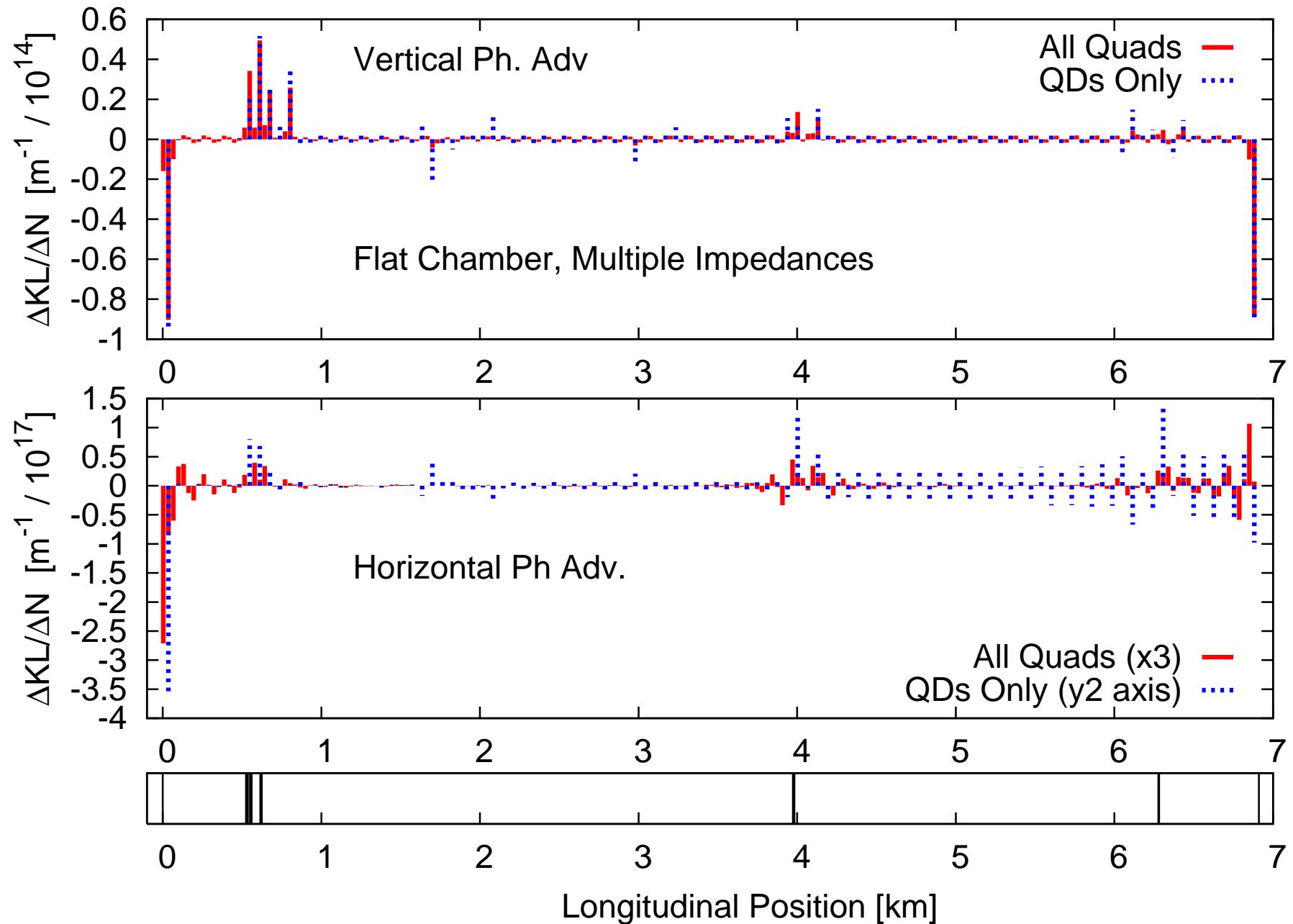
---



## Case II: Intensity Vs. $\Delta Q$ , Multiple Imps

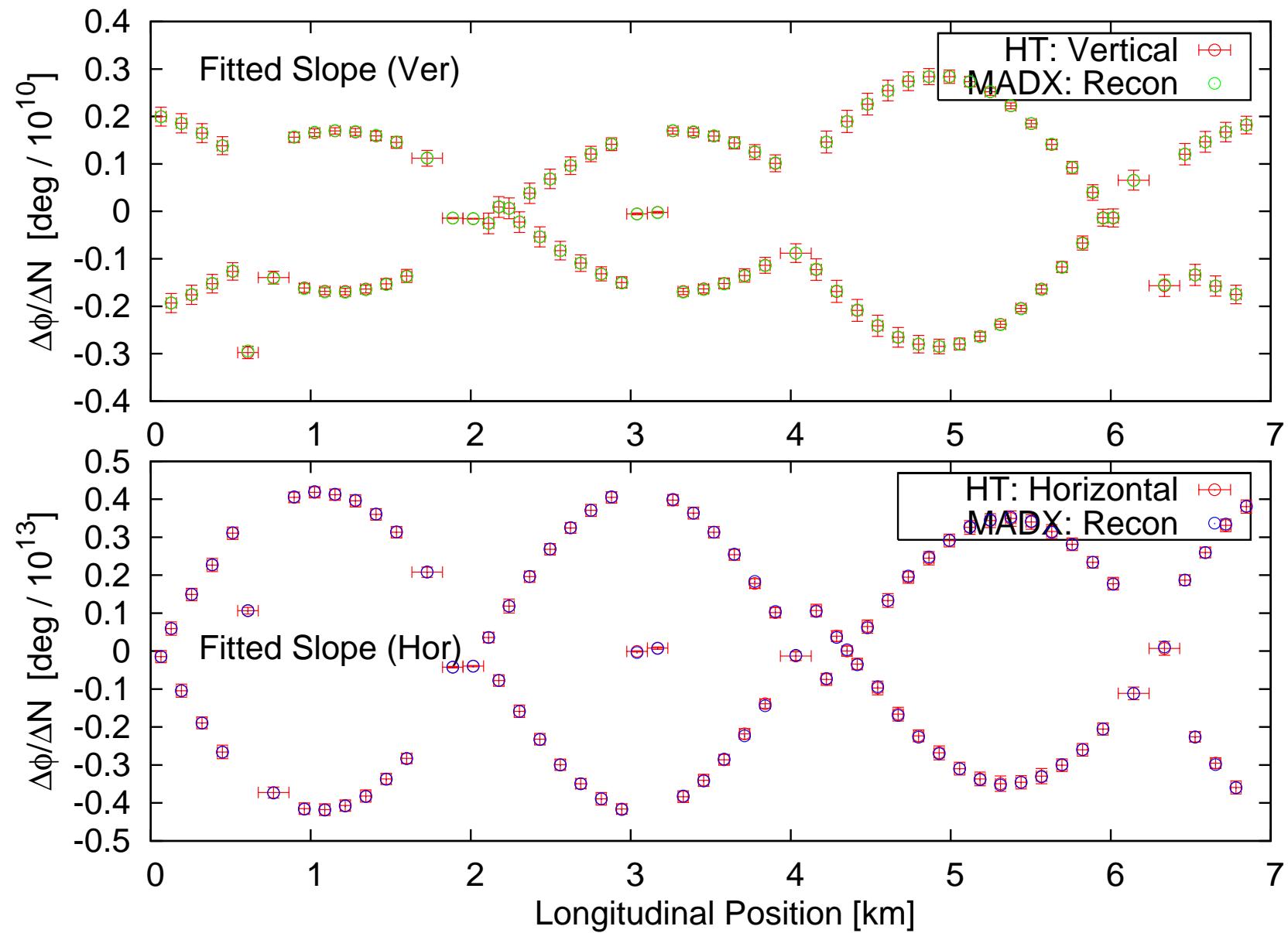


# Recon $\Delta K_i$ Sources



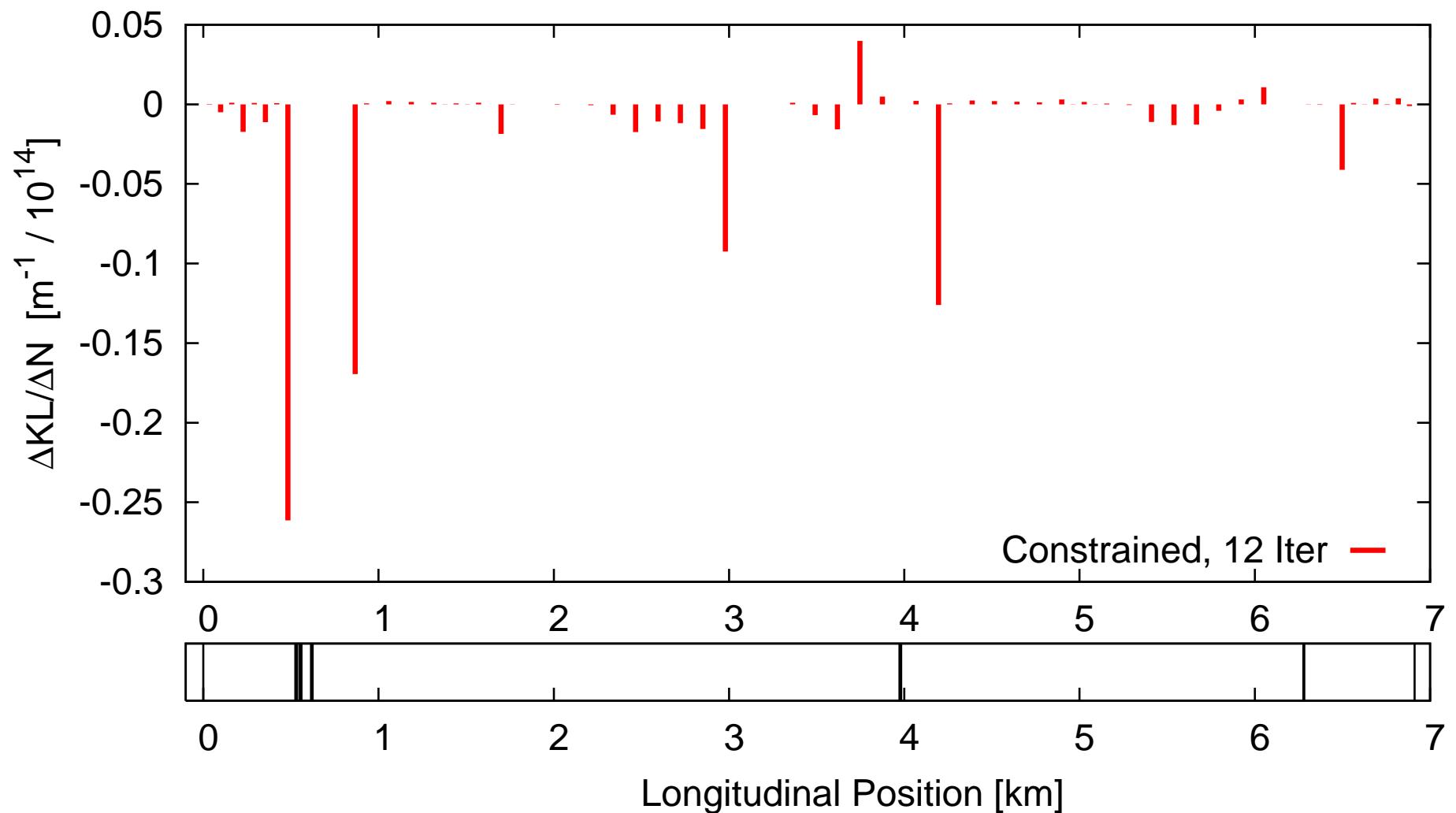
## Intensity Fitted Slope $\{\Delta\phi_{a \rightarrow b}\}$

---



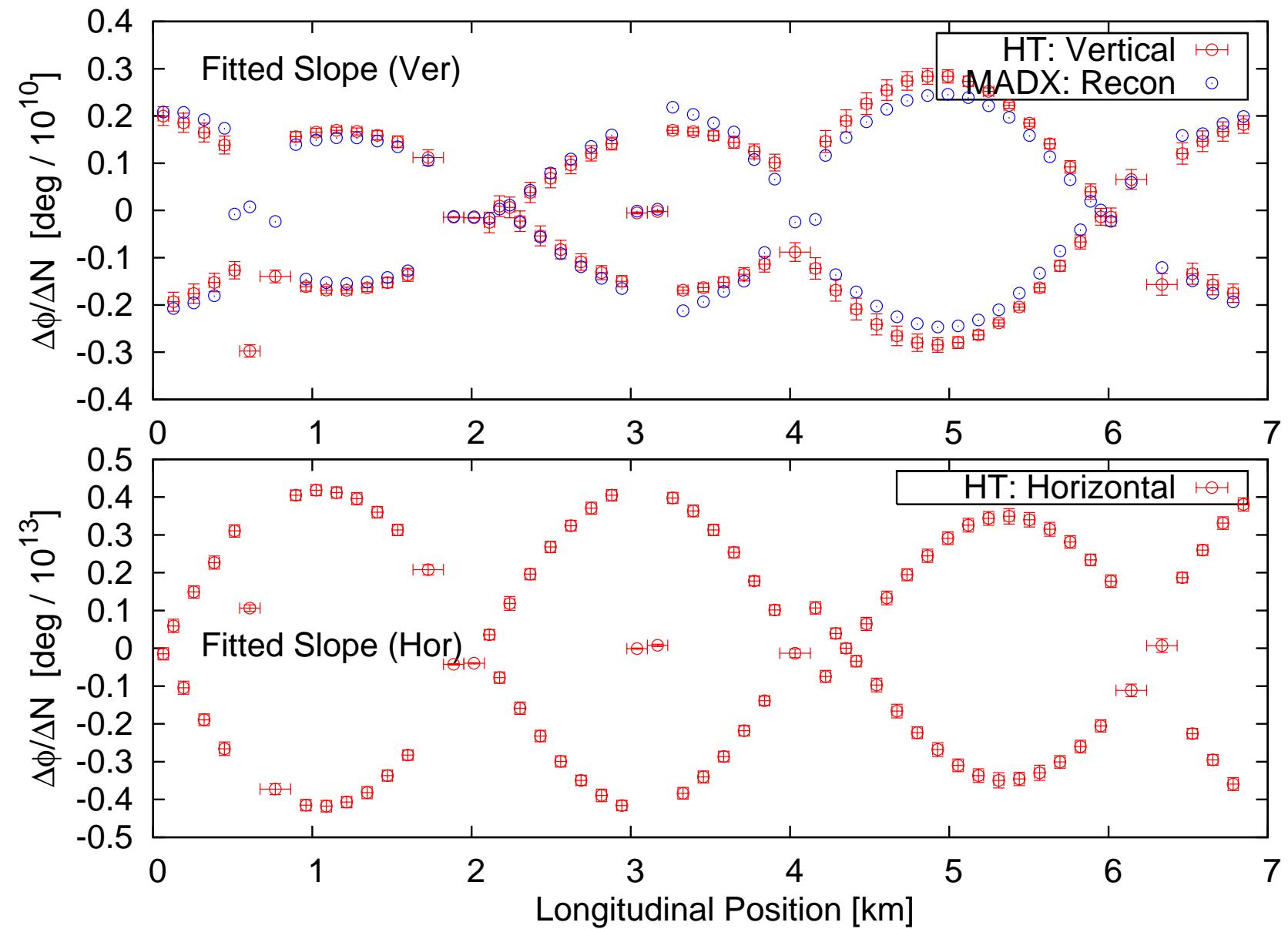
## Constrained Recon $\Delta K_i$ (Iterative)

$$[R, \vec{\lambda}I] \Delta \vec{K} = [\Delta \vec{\phi}, 0]^T \quad \{\Delta K_i < 0, \text{ QDs}\}$$



## Intensity Fitted Slope $\{\Delta\phi_{a \rightarrow b}\}$

---



## Some Key Points

---

- All quads (232) seem to reproduce a cleaner signal compared to just QDs (108)
- SVD cut to be carefully evaluated for each data set ( $2 \times 10^{-3}$ )
- “Best corrector” type algorithm is under development
- Append only vertically or horizontally focusing-defocusing matrices to each quads to expand observable space (idea from R. Tomás)
- Iteration steps only for weight determination, don’t keep previous solutions (revisit SPS data analysis)