

# Measurement of the SPS low frequency longitudinal impedance: second attempt

12 December 2007

Results of MD on 1.11.2007 and their comparison with measurements done on 20.07.2007 and in 2006

Part I: measurements based on PD signal

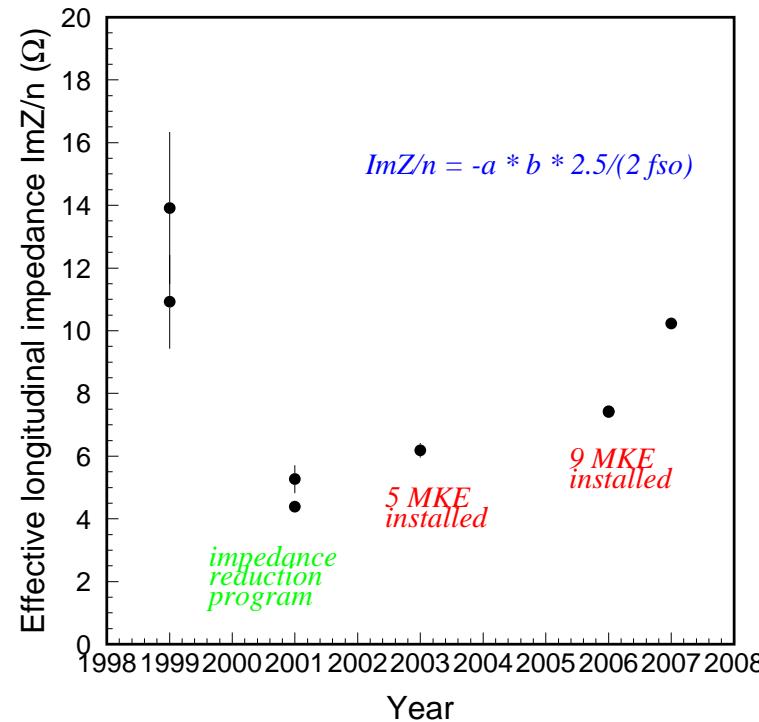
Part II: measurements based on MR data → Thomas

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Acknowledgments: G. Arduini, E. Metral and OP shift

# History and motivation

## Low frequency longitudinal inductive effective impedance



- Reduction in impedance, expected in 2007 due to removal of one MKE kicker and partial shielding of another one, **was not observed** during MD on 20.07.2007 → second attempt on 1.11.2007

## Estimation of impedance from quadrupole frequency shift:

$$\omega_2(N) = \Delta\omega_{inc}(N) + \Delta\omega_{coh}(N) + 2\omega_s^{(0)}$$

$$\omega_2(\tau, N) = 2\omega_{s0} \left\{ 1 - \frac{(\omega_{rf}\tau)^2}{64} + \frac{Ne\omega_0}{4\pi h V_0} Z_1 + \left(\frac{2}{\pi}\right)^{1/2} \frac{16Ne\omega_0 h^2}{V_0(\omega_{rf}\tau)^3} \left[ \left(\frac{\text{Im}Z}{n}\right)_0 - \frac{3}{16\sqrt{2}} \left(\frac{\text{Im}Z}{n}\right)_{eff}^{m=2} \right] \right\},$$

where ( $\omega_p = p\omega_0$ )

$$Z_1 \simeq \sum_{p=-\infty}^{\infty} p \text{Im}Z(\omega_p) e^{-\omega_p^2 \sigma^2 / 2},$$

and

$$\text{Im}(Z/\omega)_{eff}^m = \frac{\sum_{p=-\infty}^{\infty} h_m(\omega_p) Z(\omega_p) / \omega_p}{\sum_{p=-\infty}^{\infty} h_m(\omega_p)},$$

The spectral density for a Gaussian bunch:  $h_m(\omega) = (\omega\sigma)^{2m} e^{-\omega^2 \sigma^2}$

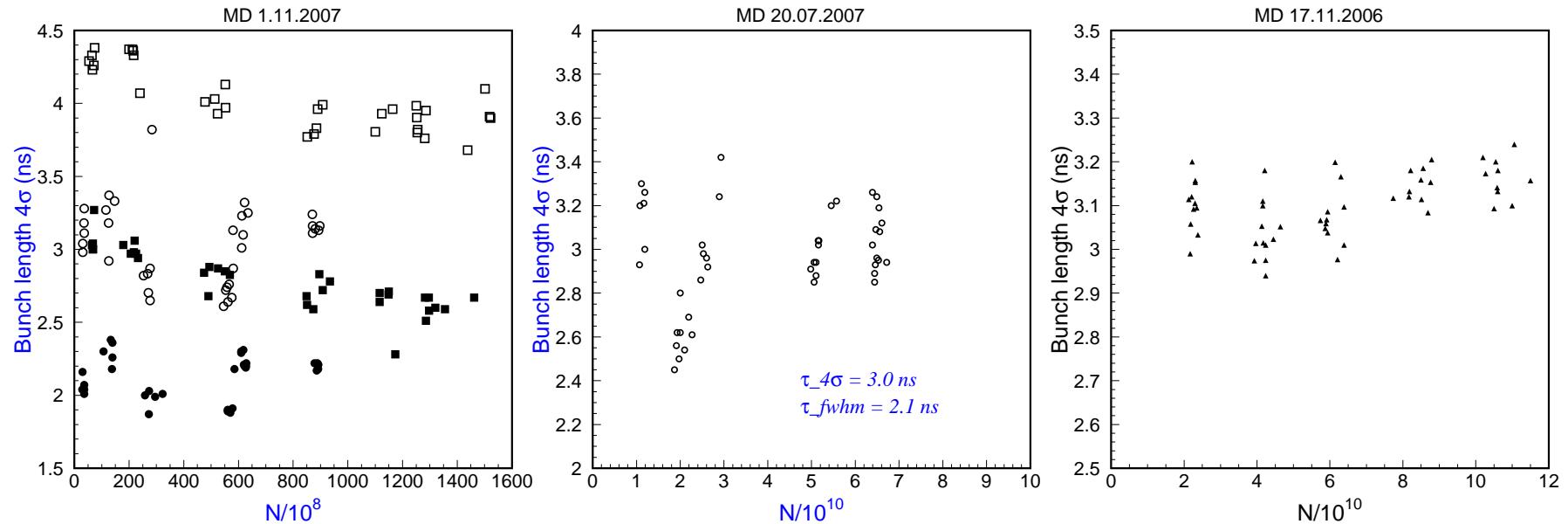
- Complicated dependence on bunch length  $\Rightarrow$  the same experimental conditions are essential for comparison

# Experimental conditions

Requirements: single bunch with variable intensity and **constant longitudinal parameters**

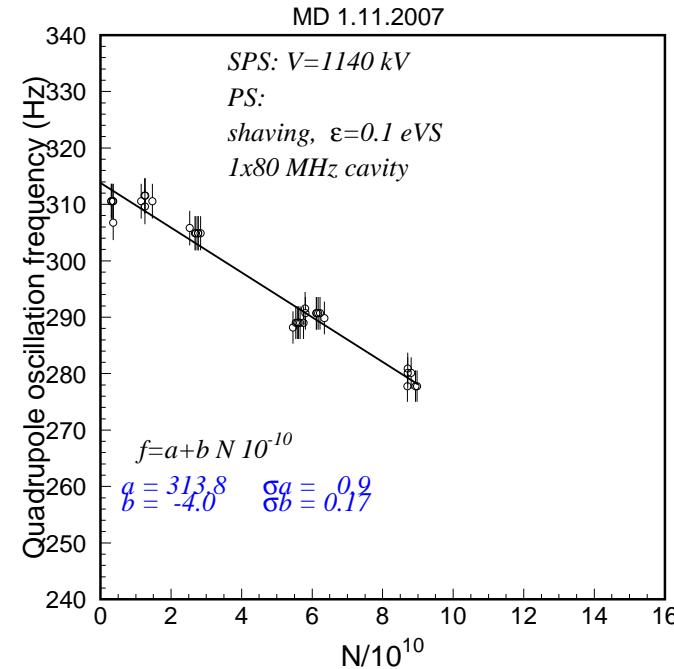
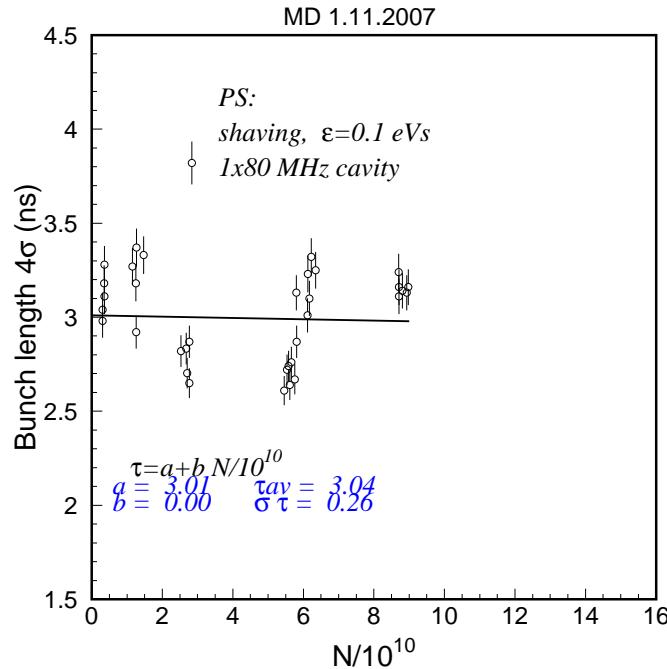
- 26 GeV/c, mismatched capture in 900 kV at 200 MHz
- measurements of **quadrupole** oscillation frequency from
  - (I) **bunch profiles** (Thomas)
    - peak amplitude oscillations
    - bunch length
    - + **intensity** measurement from BCT and calibrated peak amplitude
  - (II) **peak detected signal**
    - peak amplitude oscillations
    - + **intensity** measurement from BCT
    - + simultaneous **bunch length** measurement

## (II) Bunch length ( $4\sigma$ Gaussian fit) as a function of intensity (measured in the PS)



- 2006:  $\tau_{av} = 3.1 \text{ ns}$  and  $\varepsilon \sim 0.2 \text{ eVs}$  (long. shaving in PS from 0.3 eVs)
- 20.07.2007:  $\tau_{av} = 3.0 \text{ ns}$  and  $\varepsilon \sim 0.1 \text{ eVs}$  - long. shaving in PS (V dip)
- 1.11.2007: with long. shaving in PS:  $\varepsilon \sim 0.1 \text{ eVs}$ , no shaving:  $\varepsilon \sim 0.2 \text{ eVs}$ ; with 1x80 MHz cavity - **long** bunches and 2x80 MHz - **short** → **4 data sets**

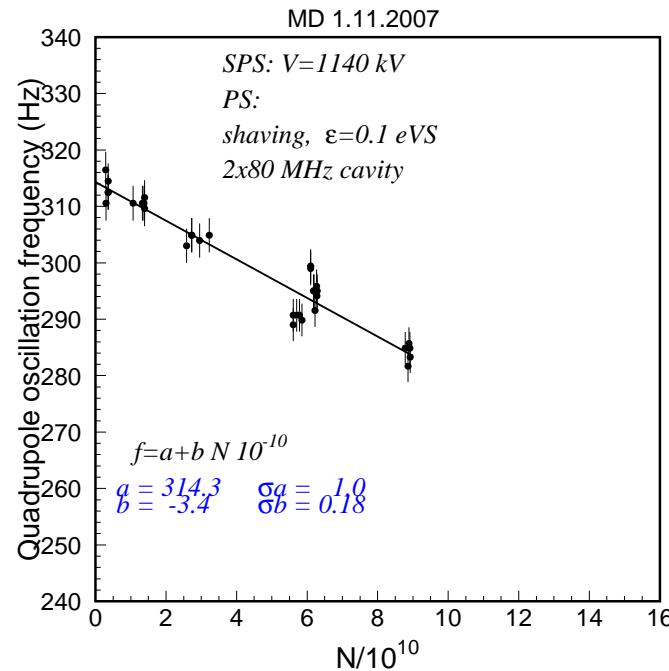
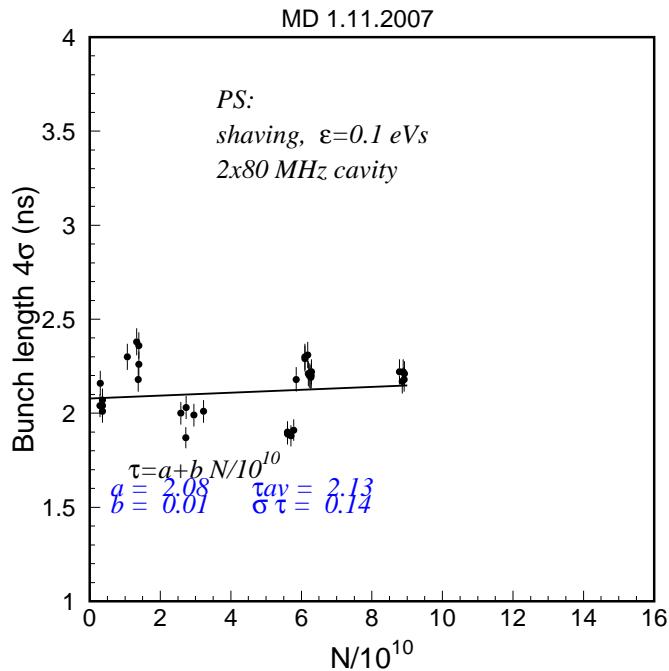
$2Q_s$  and bunch length as a function of intensity on 1.11.2007:  
 Set (11): small emittance (shaving) and long bunches (1x80 MHz)



$\Rightarrow \tau = 3.04 \pm 0.26$  ns and  $b = -4.0 \pm 0.2$  - close to 2007

## $2Q_s$ and bunch length as a function of intensity on 1.11.2007

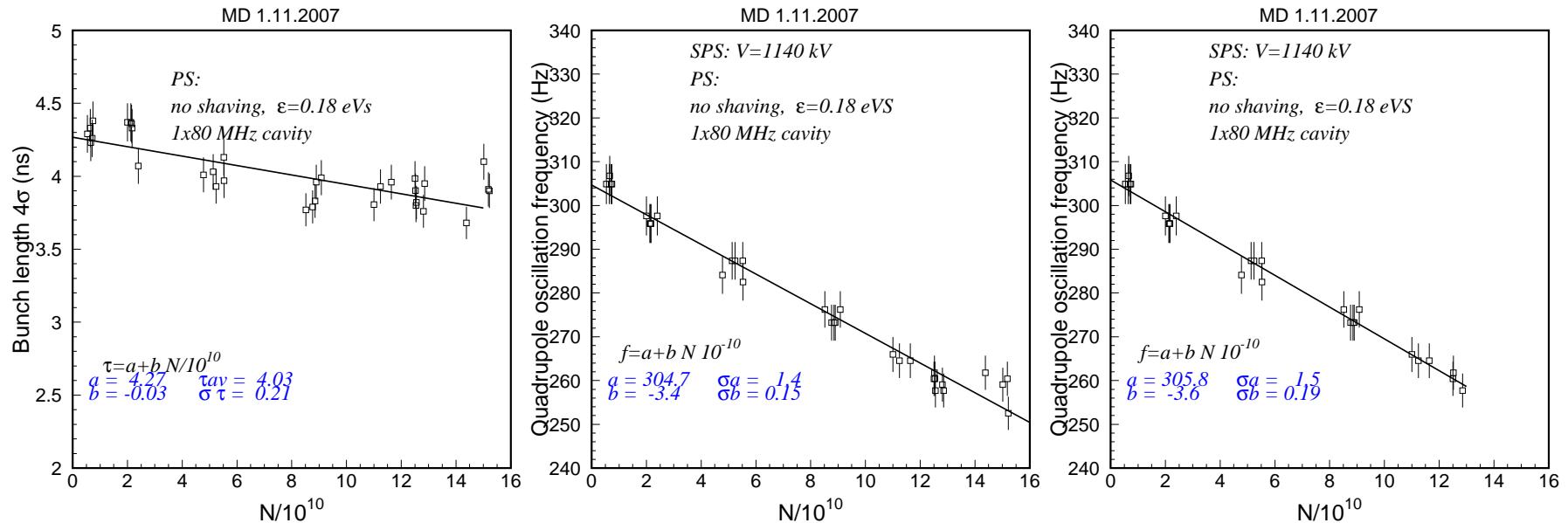
Set (12): small emittance (shaving) and short bunches (2x80 MHz)



$$\Rightarrow \tau = 2.13 \pm 0.14 \text{ ns} \text{ and } b = -3.4 \pm 0.18$$

# $2Q_s$ and bunch length as a function of intensity on 1.11.2007

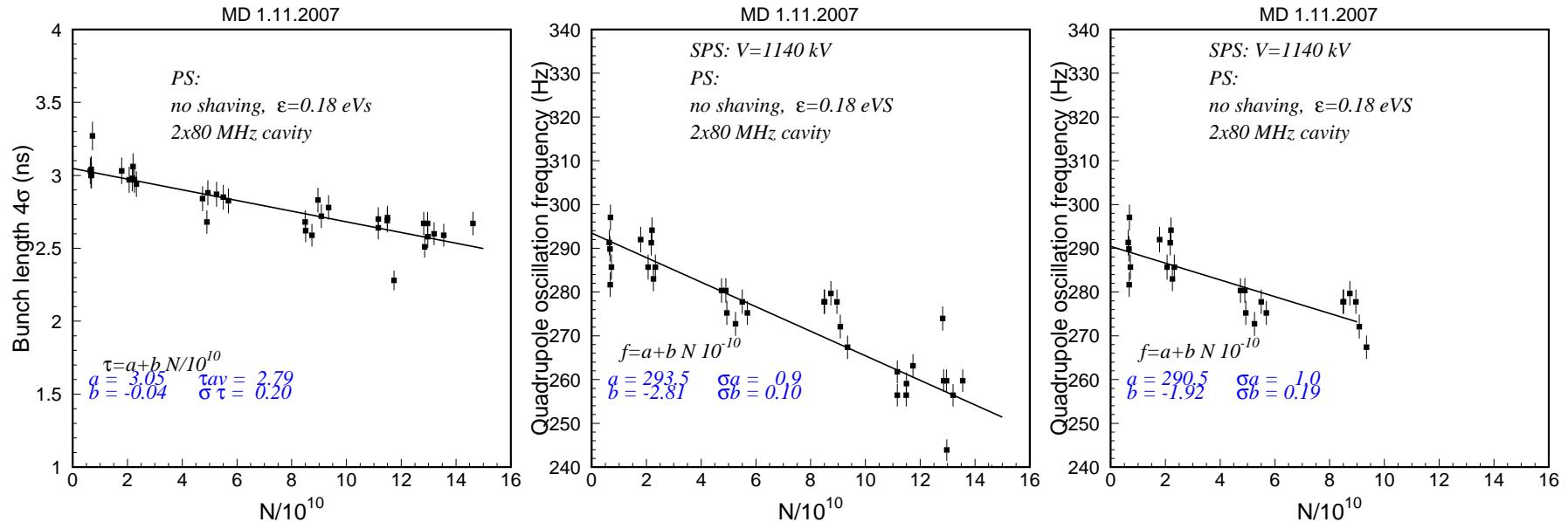
Set (21): large emittance (no shaving) and long bunches (1x80 MHz)



$$\Rightarrow \tau = 4.03 \pm 0.21 \text{ ns} \text{ and } b = -3.4 \pm 0.15$$

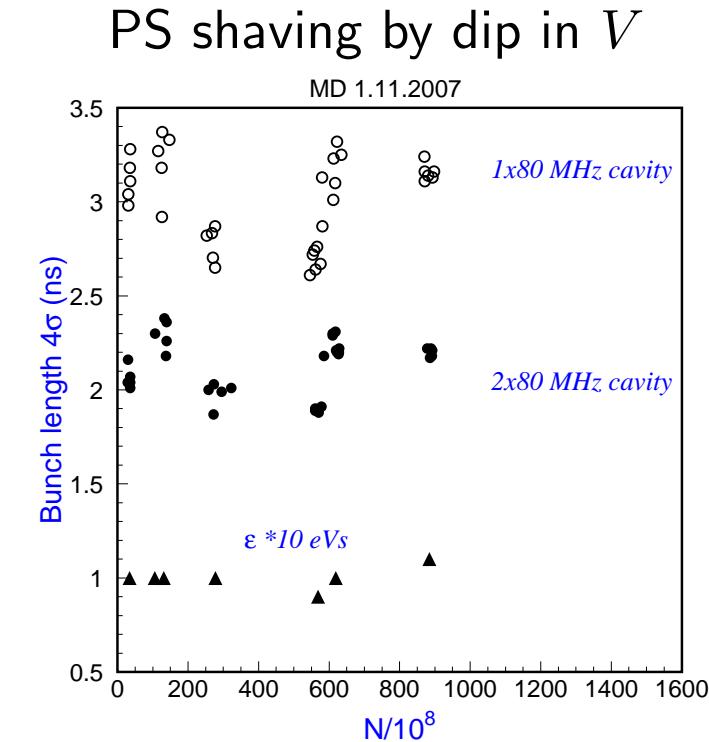
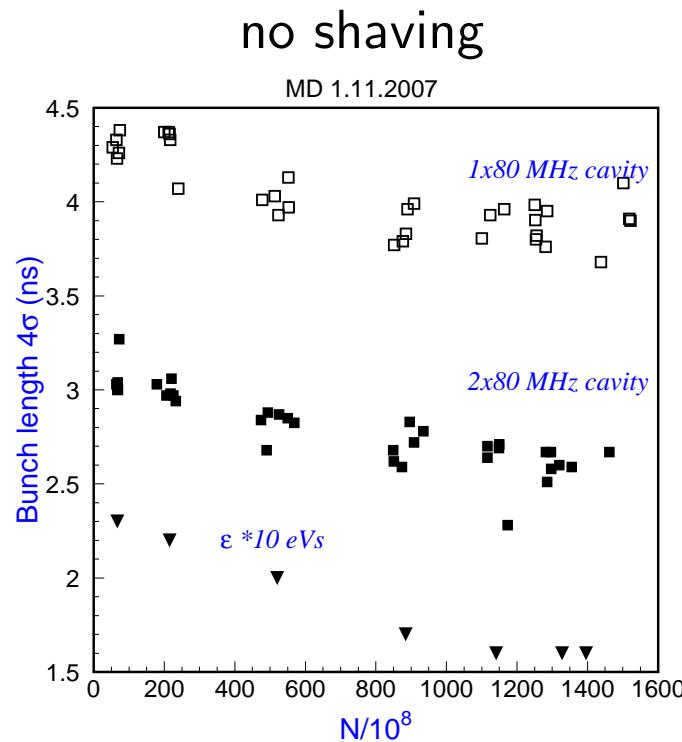
## $2Q_s$ and bunch length as a function of intensity on 1.11.2007

Set (22): large emittance (no shaving) and short bunches (2x80 MHz)



$\Rightarrow \tau = 2.8 \pm 0.2 \text{ ns}$  and  $b = -2.8 \pm 0.1$  - most close to 2006 (bunch length and emittance), but large negative (!) slope and scatter

## $\varepsilon_L$ and $\tau$ measured in the PS as a function of intensity



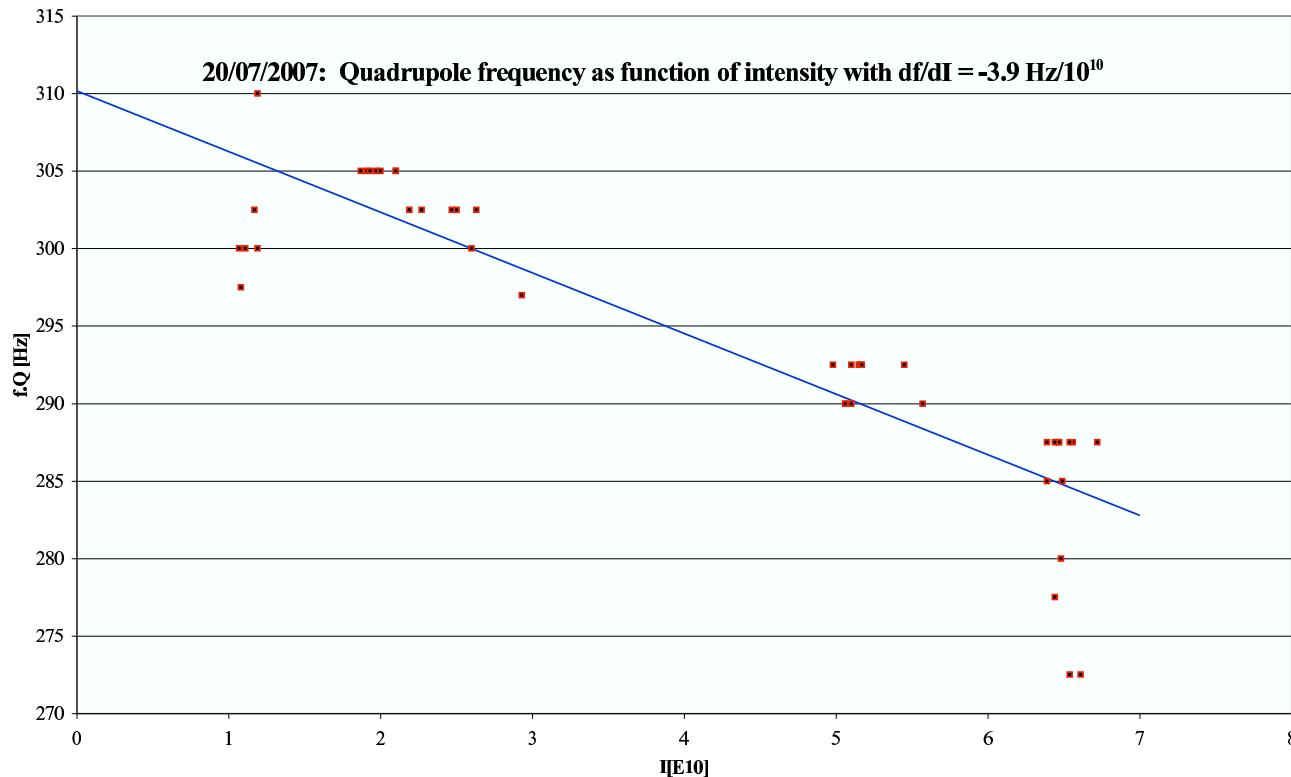
⇒ Longitudinal emittance in the PS is decreasing with intensity - **why?**

⇒ Shaving **reduces** the slope but **increases** the scatter

## (II) Measurements of quadrupole frequency shift

PD signal - FFT with dynamic signal analyzer

(measurements start 1 s after injection, acquisition time 400 ms)

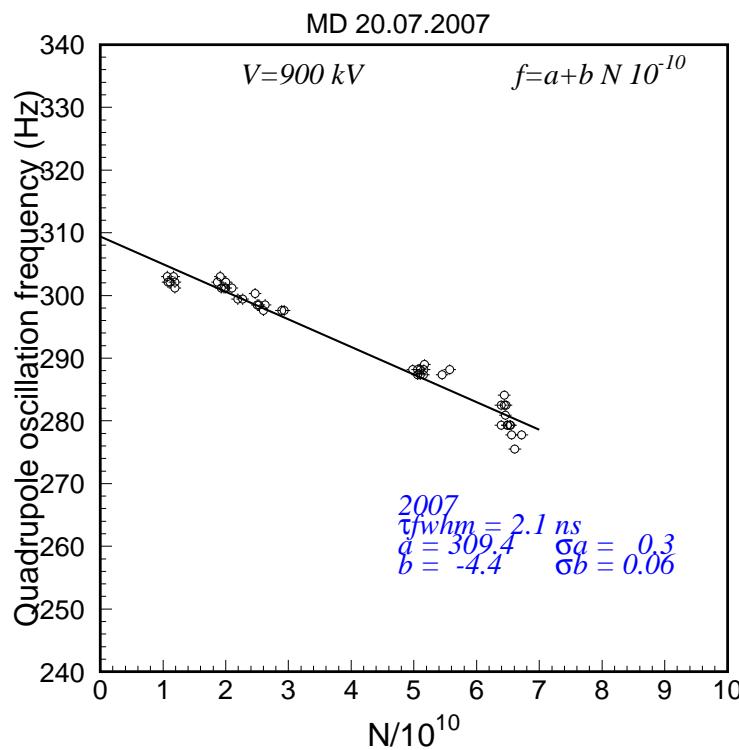


$$a = 310 \text{ Hz}, b = -3.9 \pm 0.07 \text{ Hz}$$

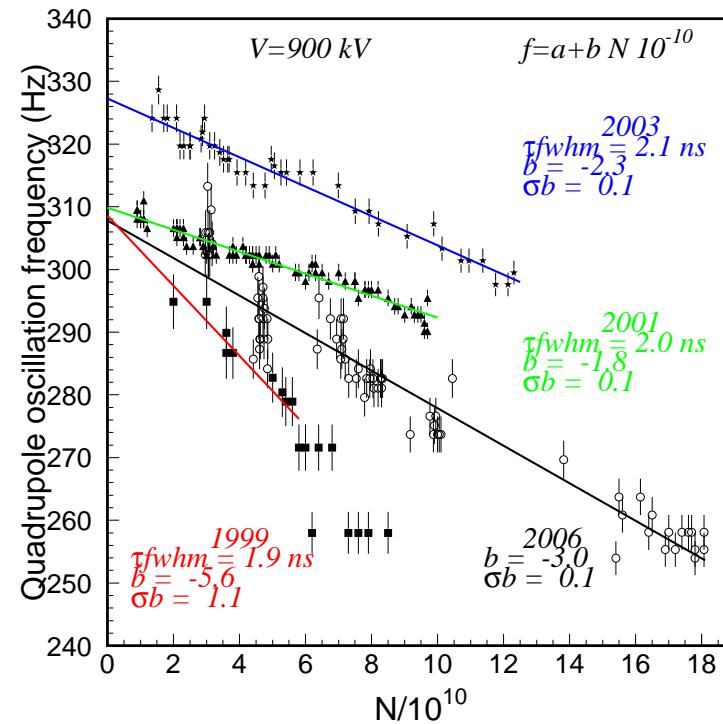
## (II) Measurements of quadrupole frequency shift

PD signal: first 5-10 oscillations on the scope

2007



1999-2006



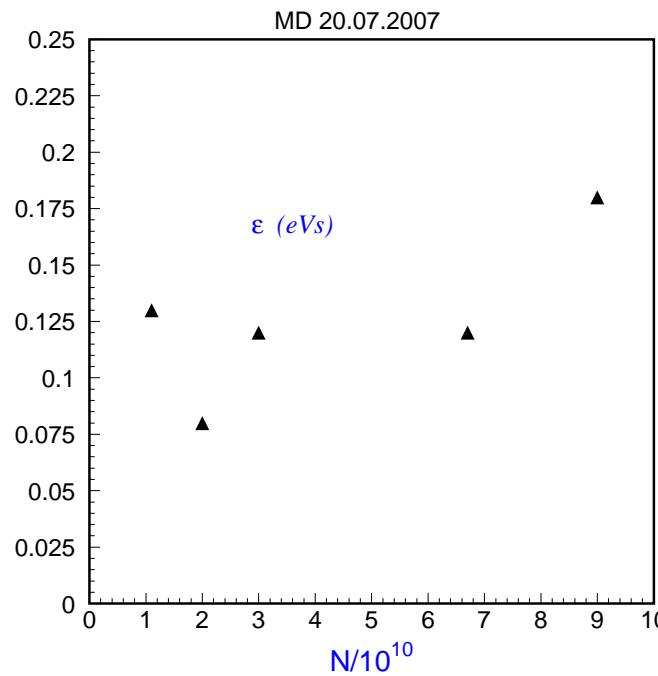
## Measurements in 2006 and 2007

MD date	$\varepsilon$ [eVs]	$n_{cav}$ in PS	$\tau_{av}$ [ns]	$ b $ from		
				MR inj.	PD inj.	PD 1 s
27.10.06	0.2-0.3	2	3.1?	3.0	2.9	3.0
17.11.06	0.25	2	3.1	3.0	3.0	3.0
20.07.07	0.08-0.18	1&2	3.0	4.5	4.4	3.8

MD on 1.11.2007

data set	$\varepsilon$ [eVs]	$n_{cav}$ in PS	bunch length [ns]		$ b $ from PD at	
			$\tau_{av} \pm D\tau$	slope	inj. (scope)	1 s (FFT)
S11	0.1	1	$3.04 \pm 0.26$	0.00	$4.0 \pm 0.2$	$3.5 \pm 0.3$
S12	0.1	2	$2.13 \pm 0.14$	0.01	$3.4 \pm 0.2$	$3.5 \pm 0.1$
S21	0.19	1	$4.03 \pm 0.21$	- 0.03	$3.4 \pm 0.2$	$2.3 \pm 0.2$
S22	0.19	2	$2.8 \pm 0.12$	- 0.04	$2.8 \pm 0.1$	$2.1 \pm 0.2$

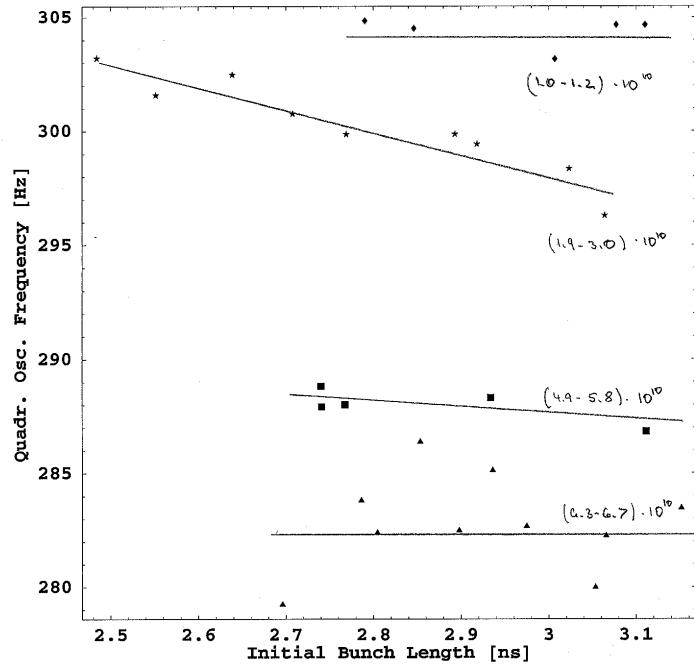
$\varepsilon_L$  measured in the PS as a function of intensity  
MD on 20.07.2007



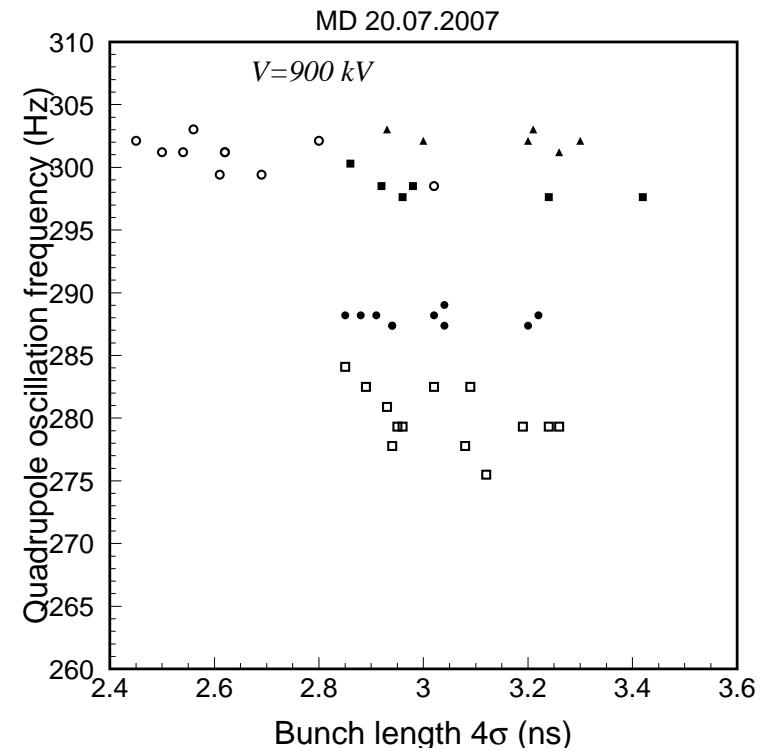
- With shaving in the PS by voltage dip

# Dependence of quadrupole frequency on bunch length

(I) - bunch profile



(II) - PD signal



⇒ No significant dependence of quadrupole frequency on bunch length for fixed intensity (and emittance?)

## Summary of $2Q_s$ measurements at the last MD (1.11.2007)

data set	$\varepsilon$ [eVs]	$n_{cav}$ in PS	$\tau_{av} \pm D\tau$ [ns]	$ b $ at		
				inj. (scope)	inj (MR)	1 s (FFT)
S11	0.1	1	$3.04 \pm 0.26$	$4.0 \pm 0.2$	$4.1 \pm 0.1$	$3.5 \pm 0.3$
S12	0.1	2	$2.13 \pm 0.14$	$3.4 \pm 0.2$	$3.4 \pm 0.2$	$3.5 \pm 0.1$
S21	0.19	1	$4.03 \pm 0.21$	$3.4 \pm 0.2$	$3.1 \pm 0.1$	$2.3 \pm 0.2$
S22	0.19	2	$2.8 \pm 0.12$	$2.8 \pm 0.2$	$2.2 \pm 0.3$	$2.1 \pm 0.2$

$\Rightarrow$  Results of measurements ( $b$ ) depend

- at injection - on bunch length and emittance
- at 1 s - on emittance

## Conclusions

- Results of measurements are sensitive to both bunch length and emittance
- Single bunch production changed from 2003:
  - PSB:  $h = 2 \rightarrow h = 1$
  - PS: additional longitudinal scraping needed to reduce  $\varepsilon_L$  (to see quadrupole oscillations with 900 kV in the SPS)
- Beam recently used for quadrupole frequency measurements did not satisfy requirements of constant  $\varepsilon_L$  and  $\tau$
- Measurements in 2006 and on 20.07.2007 were done with different  $\varepsilon_L$
- Accurate comparison with 2006 and 2001 could be done in 2008 with corresponding  $\varepsilon_L$  and  $\tau$ . Requires careful production and monitoring.